

Concrete Shear Wall Design

BY WIRA TJONG, S.E

INTRODUCTION

IR. WIRA TJONG, MSCE, SE

- ◆ **Front End Engineer of Fluor Enterprises' Tucson Office, with Experience in Indonesia, USA, Korea, Taiwan, and Malaysia as Expatriate**
- ◆ **Christian University of Indonesia (BS and ENGINEER); Virginia Tech (MS), USA; University of Wales, Swansea, UK (PhD Research Program)**
- ◆ **Licensed Structural Engineer in AZ, UT, and CA.**
- ◆ **Area of Expertise**
 - **Codes Requirements and Applications**
 - **Seismic Design for New Buildings/Bridges and Retrofit**
 - **Modeling and Software Development**
 - **Biotechnology and Microelectronic Facilities**
 - **California School and Hospitals**

ELEMENTS OF WALL DESIGN

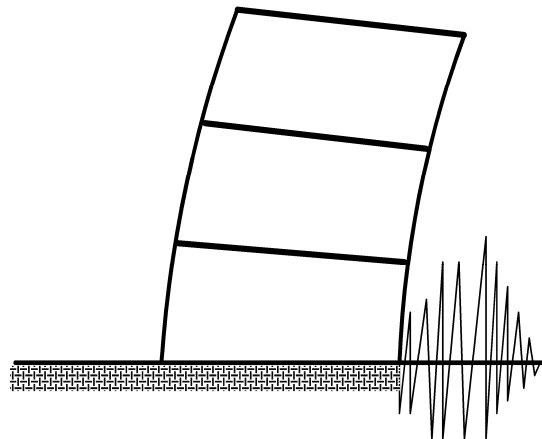
97 UBC AND 2002 ACI REQUIREMENTS FOR WALL DESIGN WITH EMPHASIS ON **SPECIAL CONCRETE SHEAR WALL**

- ◆ DEFINITION
- ◆ WALL REINFORCEMENT REQUIREMENTS
 - ◆ SHEAR DESIGN
 - ◆ FLEXURAL AND AXIAL LOAD DESIGN
 - ◆ BOUNDARY ZONE DETERMINATION
 - SIMPLIFIED APPROACH
 - RIGOROUS APPROACH
 - ◆ BOUNDARY ZONE DETAILING

DEFINITION

SHEAR WALL IS A STRUCTURAL ELEMENT USED TO RESIST LATERAL/HORIZONTAL/SHEAR FORCES PARALLEL TO THE PLANE OF THE WALL BY:

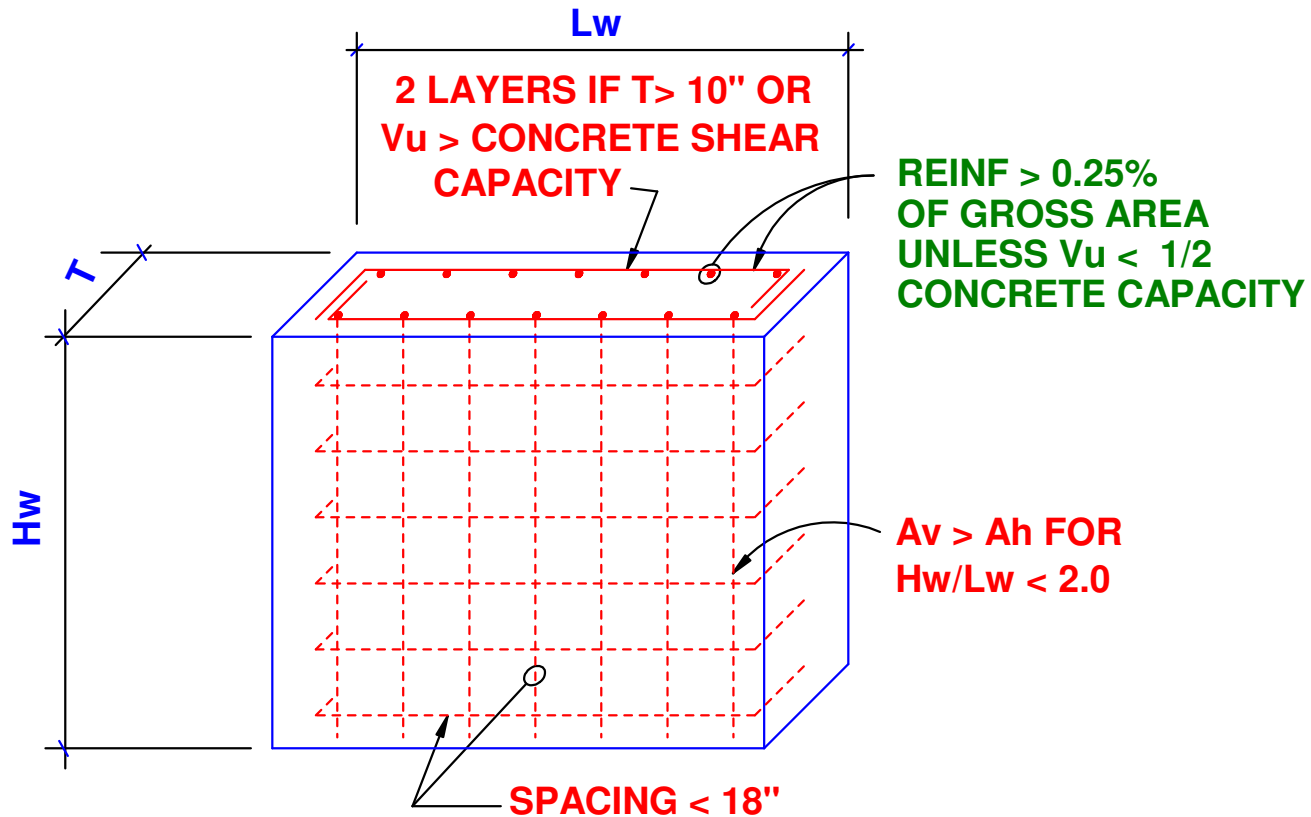
- ◆ **CANTILEVER ACTION FOR SLENDER WALLS WHERE THE BENDING DEFORMATION IS DOMINANT**
- ◆ **TRUSS ACTION FOR SQUAT/SHORT WALLS WHERE THE SHEAR DEFORMATION IS DOMINANT**



Concrete Shear Wall

WALL REINFORCEMENT

- ◆ MINIMUM TWO CURTAINS OF WALL REINFORCEMENT SHALL BE PROVIDED IF
 $V_u > 2 A_{cv}(f'c)^{1/2}$ [$0.166 A_{cv}(f'c)^{1/2}$] OR THICKNESS > 10 INCHES [25 cm]



WALL REINFORCEMENT

- ◆ WALL MINIMUM REINFORCEMENT RATIO (ρ_v or ρ_h) 0.0025
- ◆ EXCEPTION FOR $V_u < A_c v(f'c)^{1/2}$ [0.083 $A_c v(f'c)^{1/2}$]
 - a. MINIMUM VERTICAL REINFORCEMENT RATIO
 - $\rho_v = 0.0012$ FOR BARS NOT LARGER THAN #5 [⚡ 16 mm]
 - = 0.0015 FOR OTHER DEFORMED BARS
 - = 0.0012 FOR WELDED WIRE FABRIC NOT LARGER THAN W31 OR D31 [⚡ 16 mm]
 - b. MINIMUM HORIZONTAL REINFORCEMENT RATIO
 - $\rho_h = 0.0020$ FOR BARS NOT LARGER THAN #5 [⚡ 16 mm]
 - = 0.0025 FOR OTHER DEFORMED BARS
 - = 0.0020 FOR WELDED WIRE FABRIC NOT LARGER THAN W31 OR D31 [⚡ 16 mm]

SHEAR DESIGN

☠ $V_n > V_u$

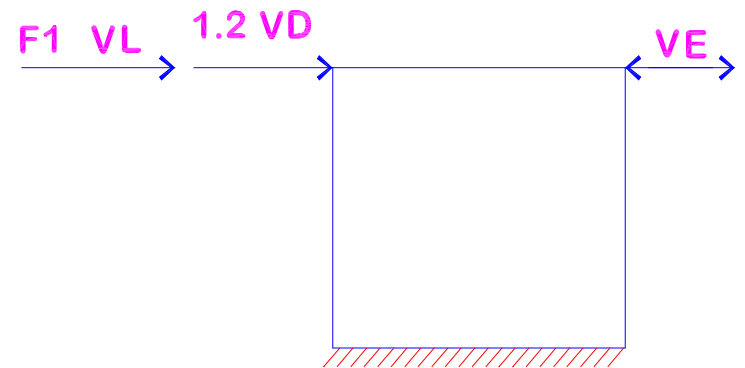
A. SHEAR DEMAND

◆ FACTORED SHEAR FORCE / SHEAR DEMAND

$$\begin{aligned} V_u &= 1.2 V_D + f_1 V_L \pm V_E \\ &= 0.9 V_D \pm V_E \end{aligned}$$

$f_1 = 1.0$ FOR 100 PSF [500 KG/M²]
LIVE LOAD AND GREATER

$f_1 = 0.5$ OTHERWISE.



SHEAR DESIGN

B. SHEAR STRENGTH

◆ NOMINAL SHEAR STRENGTH

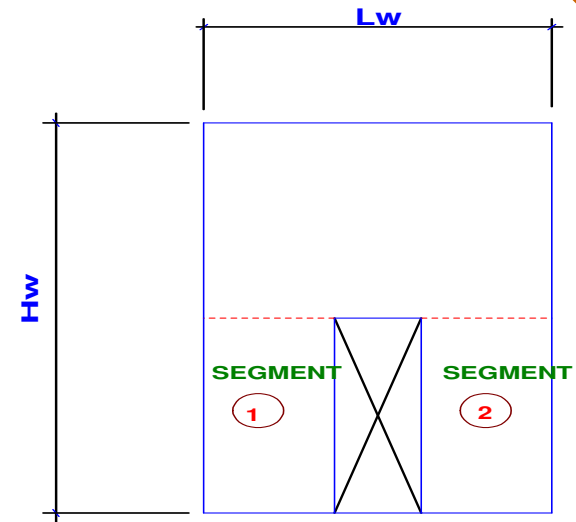
$$V_n = A_{cv} [2(f'c)^{1/2} + \rho_n f_y]$$

$$A_{cv} [0.166(f'c)^{1/2} + \rho_n f_y]$$

◆ FOR SQUAT WALLS WITH $H_w/L_w < 2.0$

$$V_n = A_{cv} [\alpha_c (f'c)^{1/2} + \rho_n f_y]$$

$$A_{cv} [0.083 \alpha_c (f'c)^{1/2} + \rho_n f_y]$$



WHERE α_c VARIES LINEARLY FROM 2.0 FOR $H_w/L_w = 2.0$ TO 3.0 FOR $H_w/L_w = 1.5$

- ◆ H_w/L_w SHALL BE TAKEN AS THE LARGEST RATIO FOR ENTIRE WALL OR SEGMENT OF WALL

SHEAR DESIGN

- ◆ MAXIMUM NOMINAL SHEAR STRENGTH

$$\text{MAX } V_n = A_{cv} [10(f'c)^{1/2}]$$

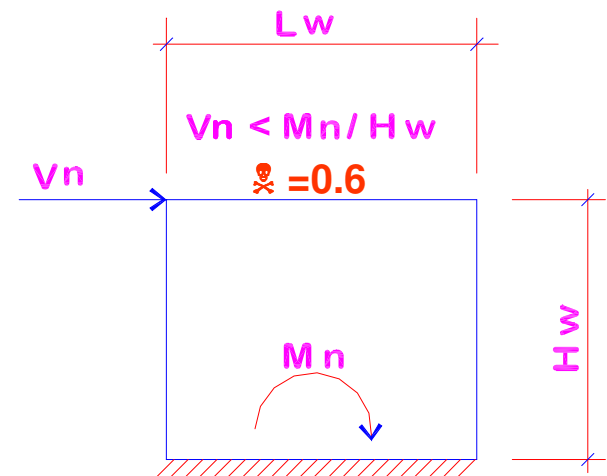
$$A_{cv} [0.83(f'c)^{1/2}]$$

- ◆ STRENGTH REDUCTION FACTOR FOR WALLS THAT WILL FAIL IN SHEAR INSTEAD OF BENDING

$$\phi = 0.6$$

- ◆ OTHERWISE

$$\phi = 0.85$$



FLEXURAL AND AXIAL LOAD DESIGN

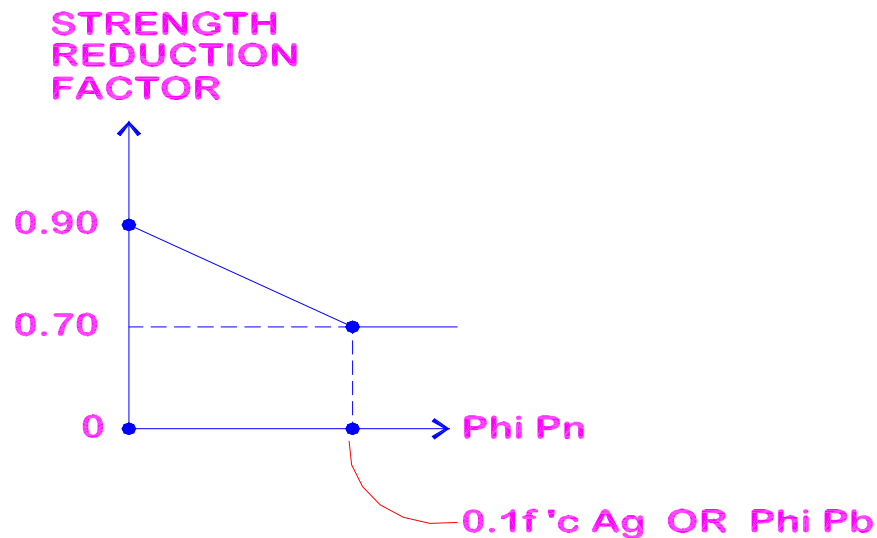
A. GENERAL

- ◆ NO NEED TO APPLY MOMENT MAGNIFICATION DUE TO SLENDERNESS
- ◆ NON-LINEAR STRAIN REQUIREMENT FOR DEEP BEAM DOESN'T APPLY

- ◆ STRENGTH REDUCTION FACTORS 0.70

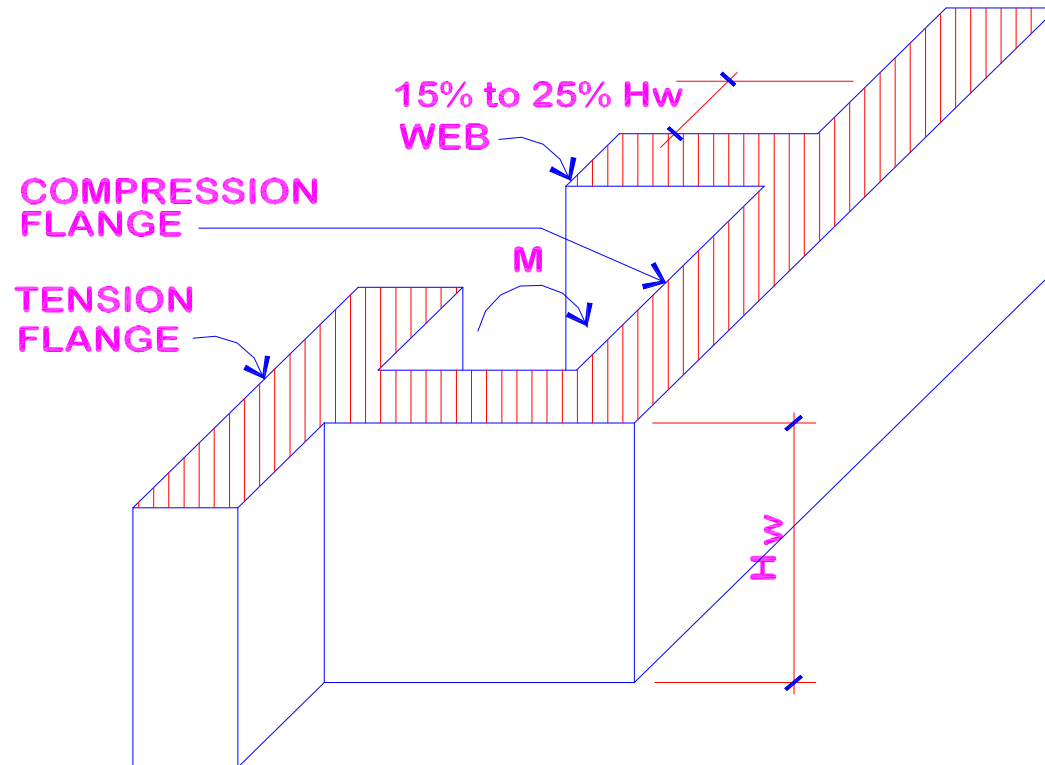
EXCEPTION FOR WALLS WITH LOW COMPRESSIVE LOAD

$\phi = 0.70$
 FOR
 $\phi P_n = 0.1f'_c A_g$ OR ϕP_b
 TO
 $\phi = 0.90$
 FOR
 $\phi P_n = \text{ZERO}$ OR TENSION



FLEXURAL AND AXIAL LOAD DESIGN

- ◆ THE EFFECTIVE FLANGE WIDTH FOR I, L, C, OR T SHAPED WALLS
 - a. 1/2 X DISTANCE TO ADJACENT SHEAR WALL WEB
 - b. 15 % OF TOTAL WALL HEIGHT FOR COMP. FLANGE (25 % PER ACI)
 - c. 30 % OF TOTAL WALL HEIGHT FOR TENSION FLANGE (25 % PER ACI)



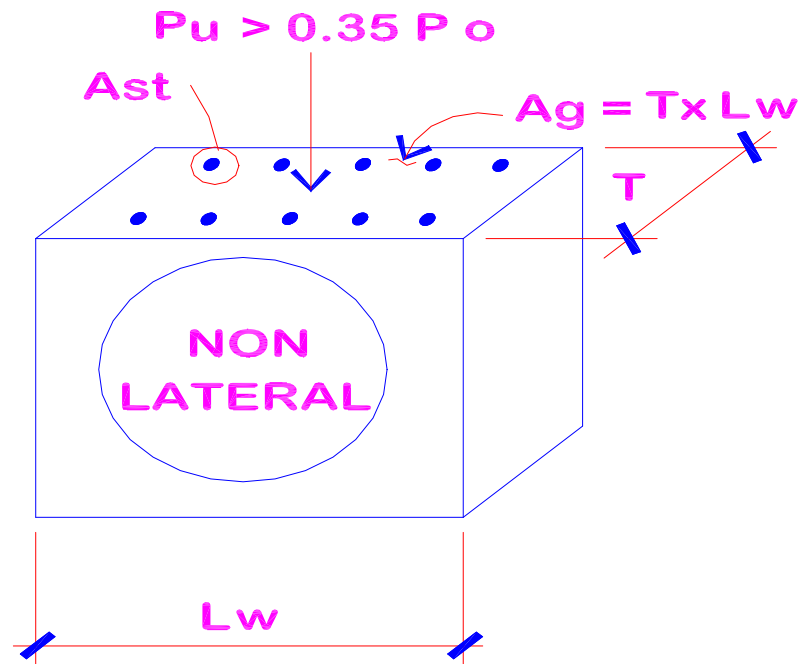
FLEXURAL AND AXIAL LOAD DESIGN

- ◆ WALLS WITH HIGH AXIAL LOAD SHALL NOT BE USED AS LATERAL RESISTING ELEMENTS FOR EARTHQUAKE FORCE IF

$$P_u > 0.35 P_o$$

WHERE

$$P_o = 0.8 \phi [0.85 f_c' (A_g - A_{st}) + f_y A_{st}]$$



B.1 BOUNDARY ZONE DETERMINATION - SIMPLIFIED APPROACH

BOUNDARY ZONE DETAILING IS NOT REQUIRED IF

◆ PER UBC :

a. $P_u \leq 0.10 A_g f'_c$ FOR SYMMETRICAL WALL

$P_u \leq 0.05 A_g f'_c$ FOR UNSYMMETRICAL WALL

AND EITHER

b. $M_u / (V_u L_w) \leq 1.0$ (SHORT/SQUAT WALL OR
 $H_w / L_w < 1.0$ FOR ONE STORY WALL)

OR

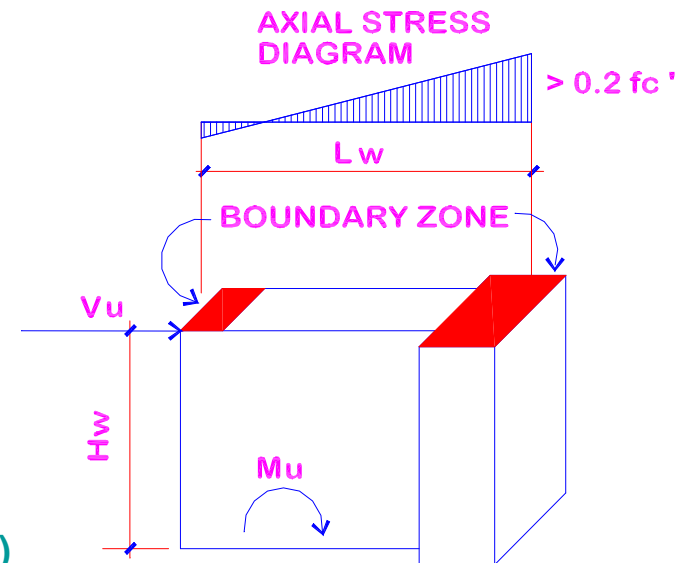
c. $V_u \leq 3 A_{cv} (f'_c)^{1/2}$ [$0.25 A_{cv} (f'_c)^{1/2}$]

AND

$M_u / (V_u L_w) \leq 3.0$

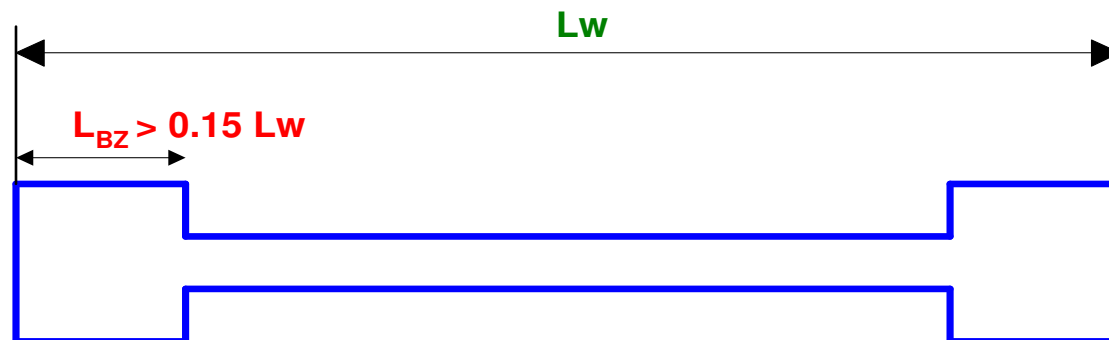
◆ PER ACI :

THE FACTORED AXIAL STRESS ON LINEAR ELASTIC GROSS SECTION $< 0.2 f'_c$



B.1 BOUNDARY ZONE DETERMINATION - SIMPLIFIED APPROACH

- ◆ IF REQUIRED, BOUNDARY ZONES AT EACH END OF THE WALL SHALL BE PROVIDED ALONG
 - ◆ $0.25L_w$ FOR $P_u = 0.35 P_o$
 - ◆ $0.15L_w$ FOR $P_u = 0.15 P_o$
- ◆ WITH LINEAR INTERPOLATION FOR P_u BETWEEN $0.15 P_o$ AND $0.35 P_o$
- ◆ MINIMUM BOUNDARY ZONE LENGTH : $0.15L_w$

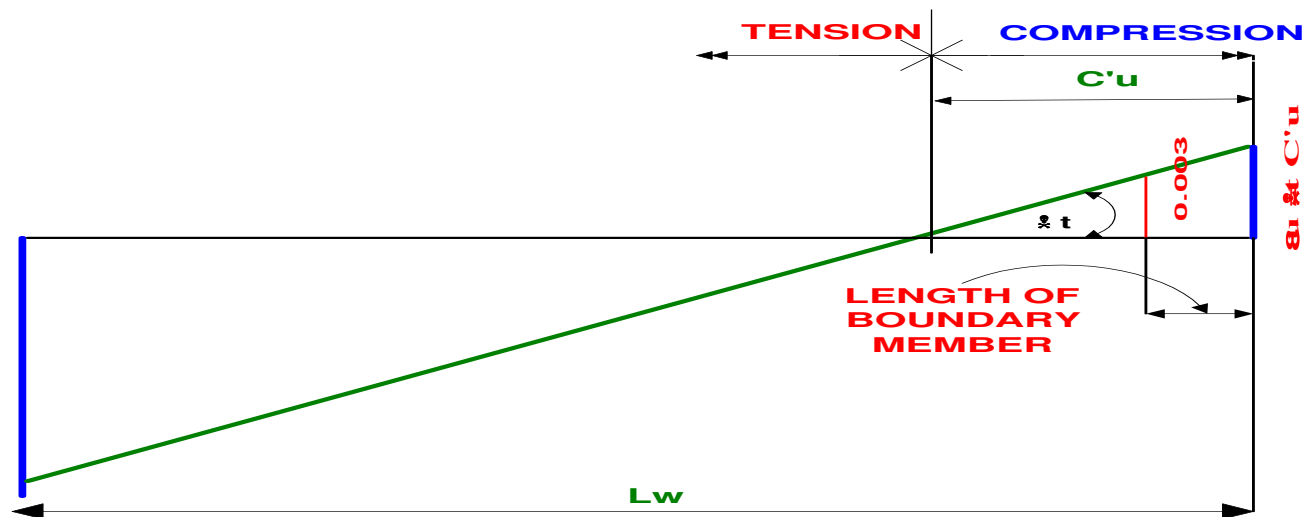


B.2 BOUNDARY ZONE DETERMINATION – RIGOROUS APPROACH

- ◆ **BOUNDARY ZONE DETAILING IS NOT REQUIRED IF MAX. COMPRESSIVE STRAIN AT WALL EDGES:**

$$\gamma_{o_{max}} < 0.003$$

- ◆ **THE DISPLACEMENT AND THE STRAIN SHALL BE BASED ON CRACKED SECTION PROPERTIES, UNREDUCED EARTHQUAKE GROUND MOTION AND NON-LINEAR BEHAVIOR OF THE BUILDING.**
- ◆ **BOUNDARY ZONE DETAIL SHALL BE PROVIDED OVER THE PORTION OF WALL WITH COMPRESSIVE STRAIN > 0.003 .**



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B.2 BOUNDARY ZONE DETERMINATION – RIGOROUS APPROACH

◆ THE MAXIMUM ALLOWABLE COMPRESSIVE STRAIN

$$\gamma_{o_{max}} = 0.015$$

- PER ACI, BOUNDARY ZONE DETAILING IS NOT REQUIRED IF THE LENGTH OF COMP. BLOCK

$$C < L_w / [600 * (\Delta_u / H_w)]$$

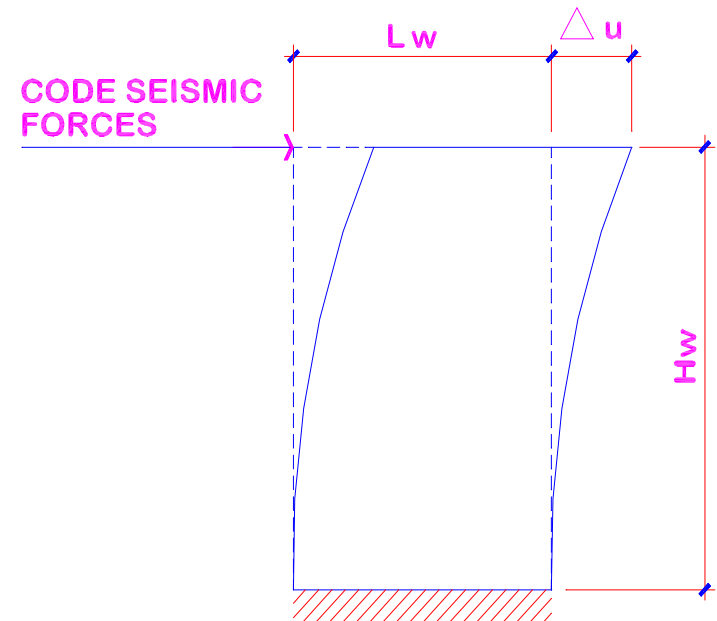
(Δ_u / H_w) SHALL NOT BE TAKEN < 0.007

- IF REQUIRED, THE BOUNDARY ZONE LENGTH SHALL BE TAKEN AS

$$L_{bz} > C - 0.1 L_w$$

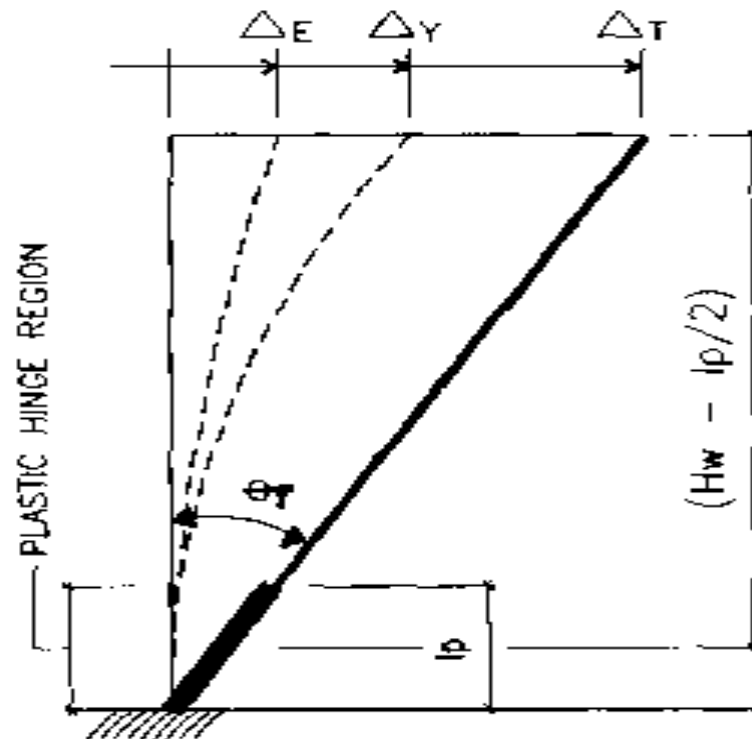
AND

$$> C/2$$



C. APPROXIMATE COMPRESSIVE STRAIN FOR PRISMATIC WALLS YIELDING AT THE BASE

- ◆ DETERMINE Δ_e : ELASTIC DESIGN DISPLACEMENT AT THE TOP OF WALL DUE TO CODE SEISMIC FORCES BASED ON GROSS SECTION PROPERTIES

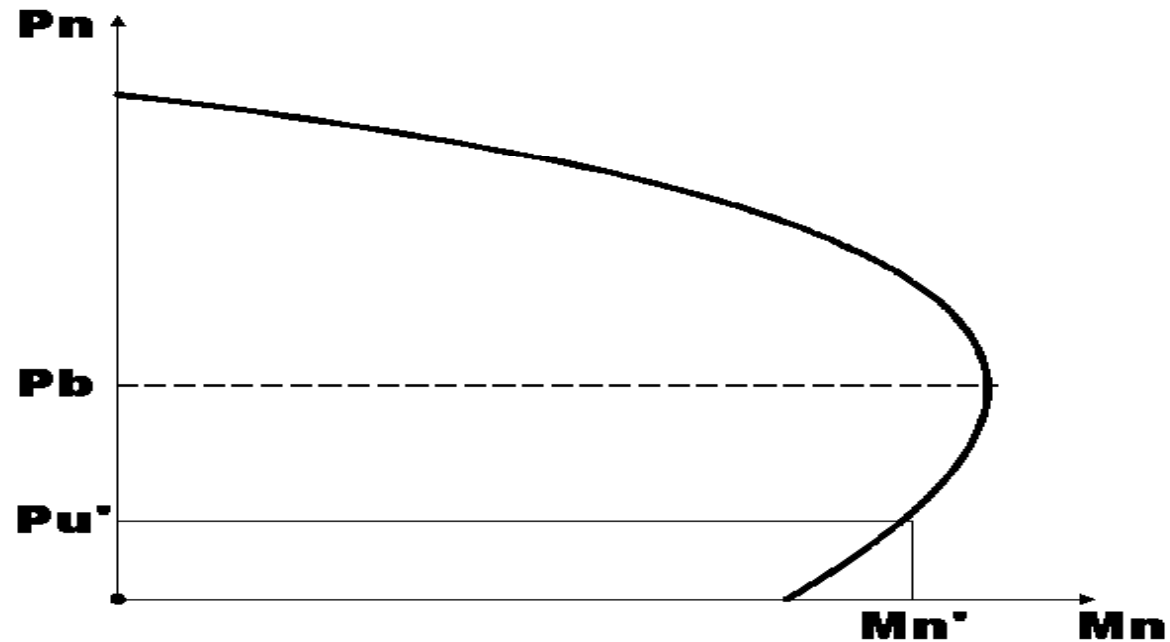


C. APPROXIMATE COMPRESSIVE STRAIN

- ◆ CALCULATE YIELD DEFLECTION AT THE TOP OF WALL CORRESPONDING TO A COMPRESSIVE STRAIN OF 0.003

$$\Delta y = (Mn'/Me)\Delta e$$

- ◆ M_e IS MOMENT DUE TO CODE SEISMIC FORCES



C. APPROXIMATE COMPRESSIVE STRAIN

- ◆ **Mn' IS NOMINAL FLEXURAL STRENGTH AT**

$$P_u = 1.2P_D + 0.5P_L + P_E$$

- ◆ **DETERMINE TOTAL DEFLECTION AT THE TOP OF WALL**

$$\Delta_t = \Delta_m = 0.7 R (2\Delta_E) \text{ BASED ON GROSS SECTION}$$

OR

$$\Delta_t = \Delta_m = 0.7 R \Delta_s \text{ BASED ON CRACKED SECTION}$$

WHERE R IS DUCTILITY COEFFICIENT RANGES FROM 4.5 TO 8.5 PER UBC TABLE 16 N.

- ◆ **INELASTIC WALL DEFLECTION**

$$\Delta_i = \Delta_t - \Delta_y$$

- ◆ **ROTATION AT THE PLASTIC HINGE**

$$\Theta_i = \frac{\Delta_i}{L_p} = \frac{\Delta_i}{(H_w - L_p/2)}$$

C. APPROXIMATE COMPRESSIVE STRAIN

- ◆ DETERMINE TOTAL CURVATURE DEMAND AT THE PLASTIC HINGE

$$\kappa_t = \kappa_i + \kappa_y$$

$$\kappa_t = \Delta i / [L_p(H_w - L_p/2)] + \kappa_y$$

- ◆ WALL CURVATURE AT YIELD OR AT M_n' CAN BE TAKEN AS

$$\kappa_y = 0.003/L_w$$

- ◆ THE PLASTIC HINGE LENGTH

$$L_p = L_w/2$$

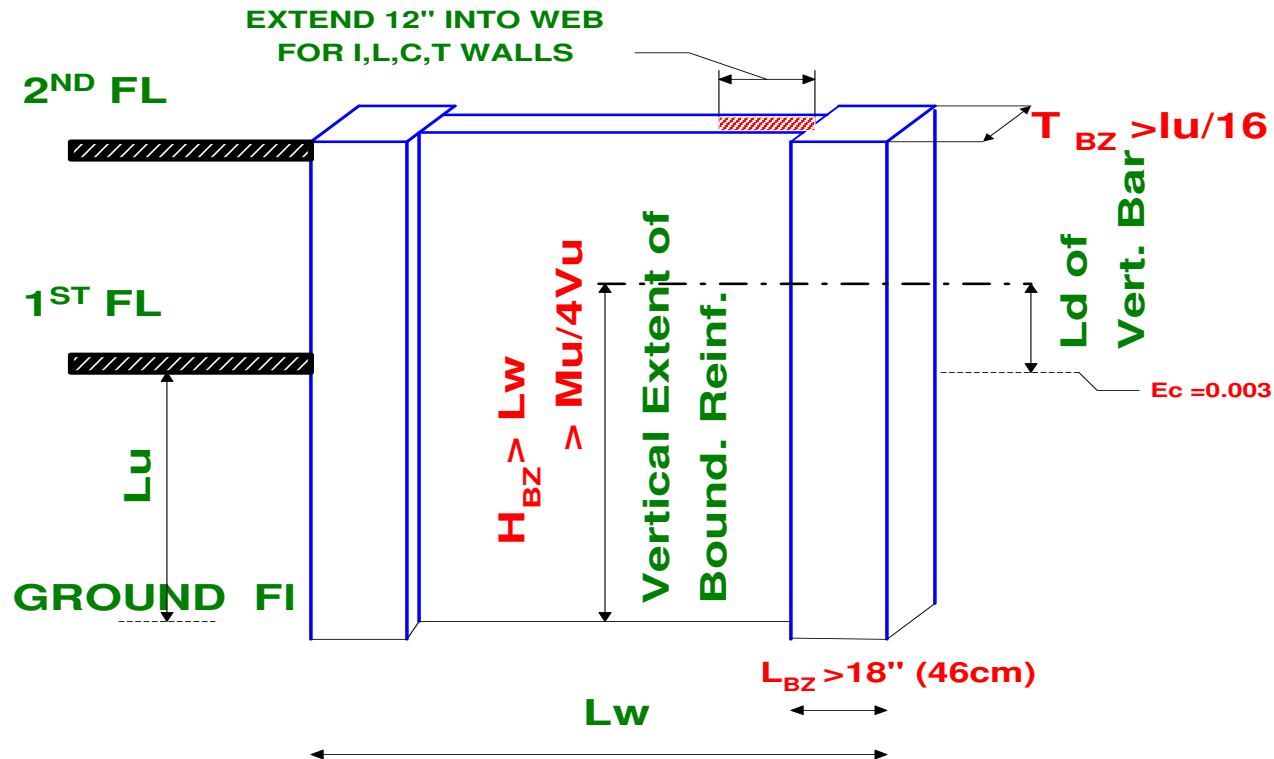
- ◆ THE COMPRESSIVE STRAIN ALONG COMPRESSIVE BLOCK IN THE WALL MAY BE ASSUMED VARY LINEARLY OVER THE DEPTH C_u' WITH A MAXIMUM VALUE EQUAL TO

$$\gamma_{o_{cmax}} = (C_u' \times \kappa_t)$$

- ◆ THE COMPRESSIVE BLOCK LENGTH C_u' CAN BE DETERMINED USING STRAIN COMPATIBILITY AND REINFORCED CONCRETE SECTION ANALYSIS.

D. BOUNDARY ZONE DETAILS

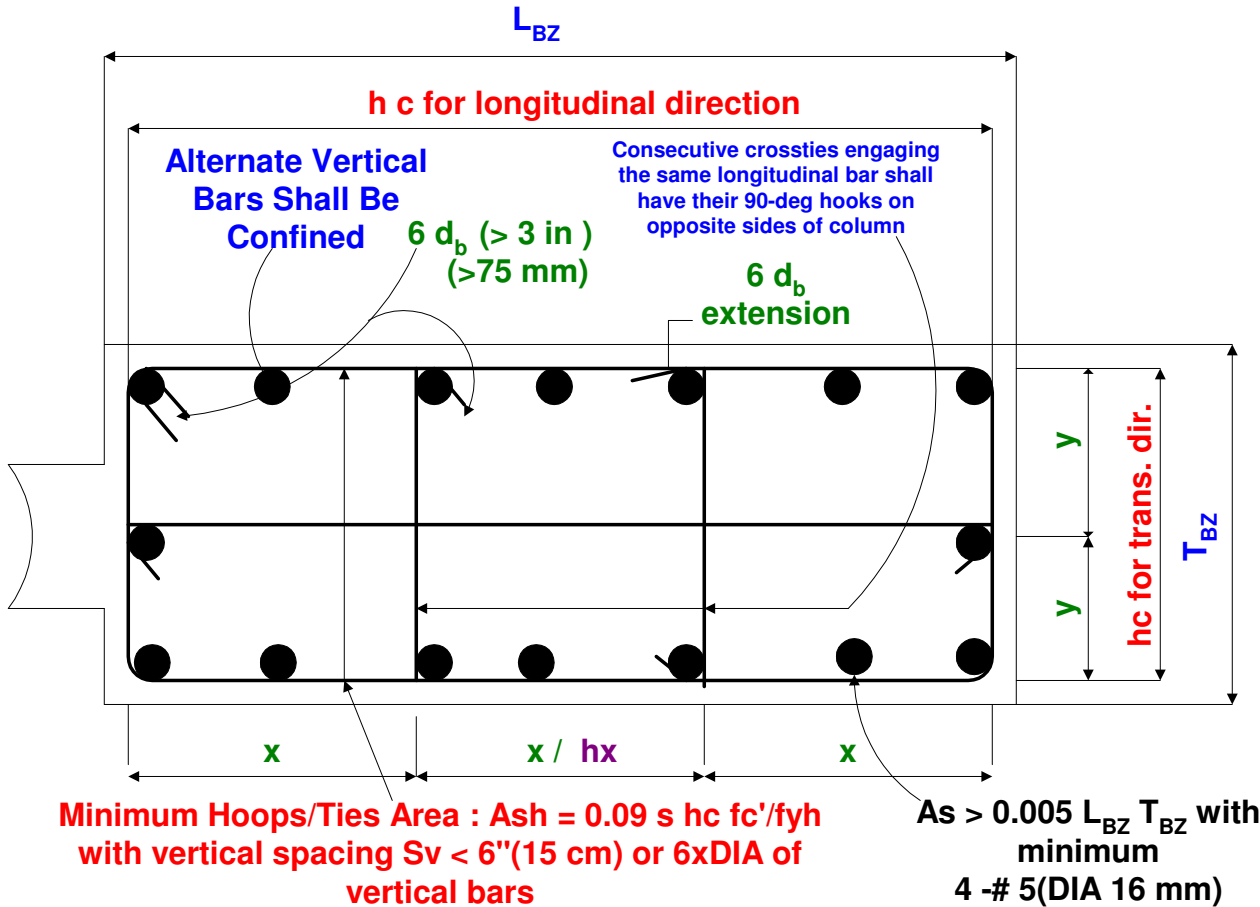
◆ DIMENSIONAL REQUIREMENTS



☞ FOR L, C, I, OR T SHAPED WALL, THE BOUNDARY ZONE SHALL INCLUDE THE EFFECTIVE FLANGE AND SHALL EXTEND AT LEAST 12 INCHES [30 CM] INTO THE WEB

D. BOUNDARY ZONE DETAILS

◆ CONFINEMENT REINFORCEMENT

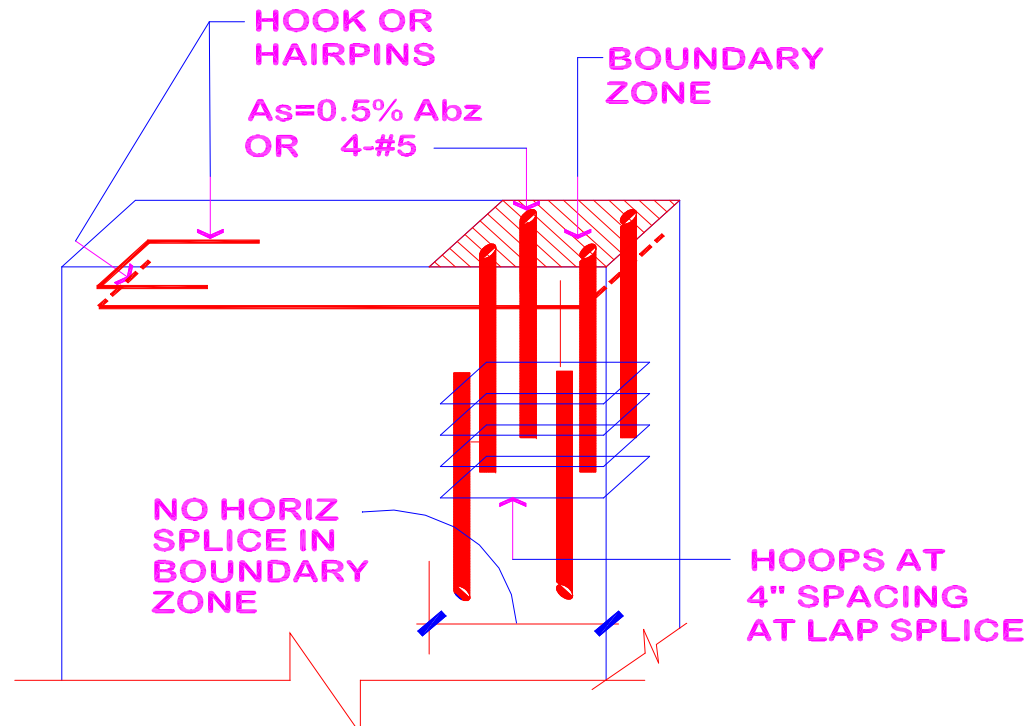


Notes:

- Per UBC:
'x' or 'y' < 12 inches (30 cm)
Per - ACI
'hx' < 14 inches (35 cm)
- Hoop dimensional ratio
(3x/2y) or (2y/3x) < 3
- Adjacent hoops shall be overlapping
- Per ACI:
 $S_v < T_{bz} / 4$
 $S_v < 4 + [(14-hx)/3]$
in inches
< 10 + [(35-hx)/3]
in cm

D. BOUNDARY ZONE DETAILS

◆ REINFORCEMENT INSIDE BOUNDARY ZONE



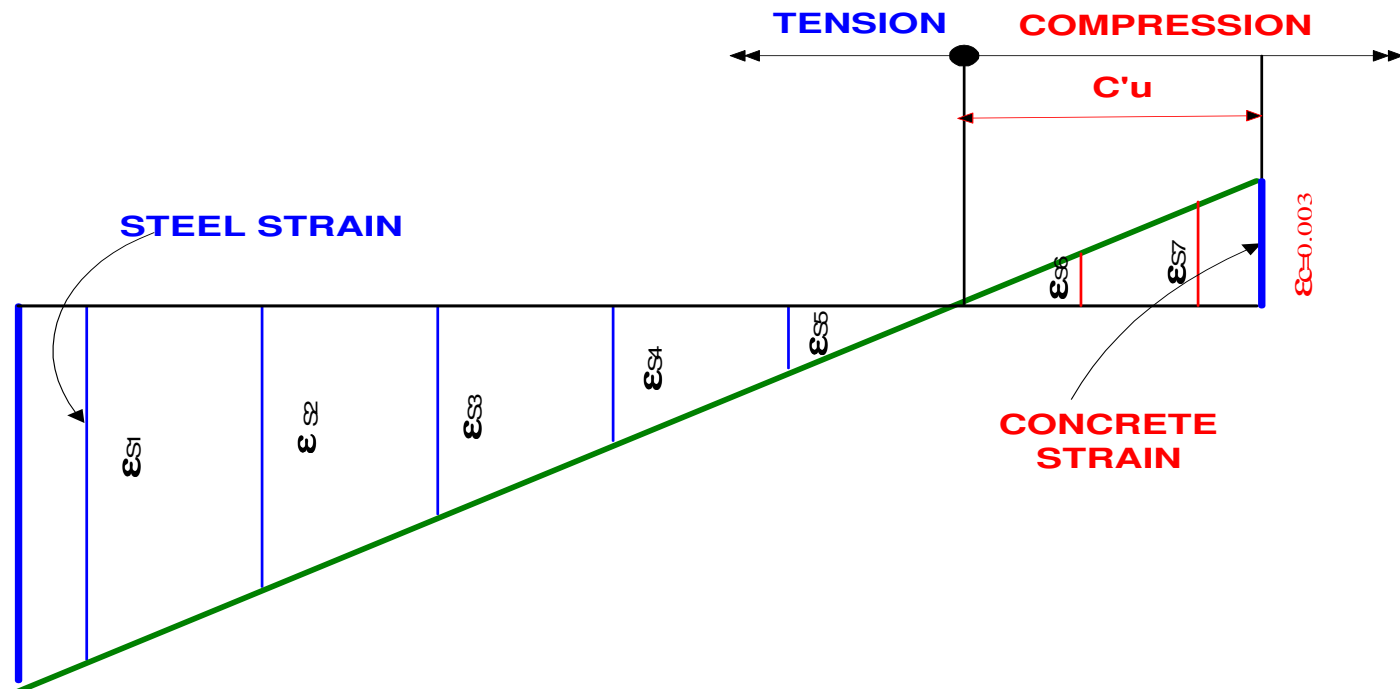
- ☞ NO WELDED SPLICE WITHIN THE PLASTIC HINGE REGION
- ☞ MECHANICAL CONNECTOR STRENGTH $> 160\%$ OF BAR YIELD STRENGTH OR $95\% F_u$

STRAIN COMPATIBILITY ANALYSIS FOR ESTIMATING M'n and C'u

◆ STRAIN DISTRIBUTION AT $\gamma_{o_{cy}} = 0.003$

$$\gamma_{o_{si}} > \gamma_{o_y} : \quad T_{si} = A_s f_y$$

$$\gamma_{o_{si}} < \gamma_{o_y} : \quad T_{si} = A_s f_s \quad \text{WHERE } f_s = E_s \gamma_{o_s}$$



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STRAIN COMPATIBILITY ANALYSIS

◆ FORCE EQUILIBRIUM

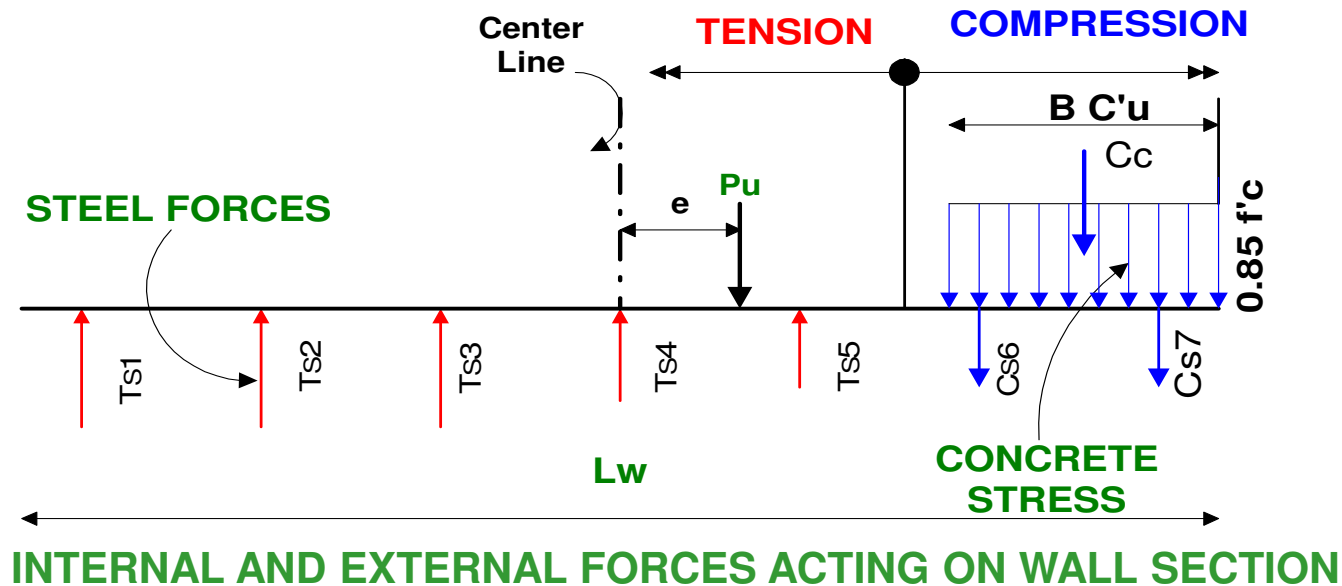
$$P_u + \sum T_{si} + \sum C_{si} + C_c = 0$$

WHERE $P_u = 1.2 D + 0.5 L + E$ AND $C_c = 0.85 f'_c B C'u$

◆ MOMENT EQUILIBRIUM

$$M'n = \sum T_{si} X e_{si} + \sum C_{si} X e_{si} + C_c e_c$$

◆ SOLVE FOR C_u' THAT SATISFIES THE ABOVE EQUILIBRIUM.



SUMMARY

- ◆ TWO APPROACHES TO DETERMINE THE BOUNDARY ZONE
- ◆ THE SIMPLIFIED APPROACH IS BASED ON THE AXIAL FORCE, BENDING AND SHEAR OR FACTORED AXIAL STRESSES IN THE WALL
- ◆ THE RIGOROUS APPROACH INVOLVES DISPLACEMENT AND STRAIN CALCULATIONS
- ◆ ACI/IBC EQUATIONS ARE SIMPLER THAN UBC EQUATIONS
- ◆ COMPUTER AIDED CALCULATIONS ARE REQUIRED FOR THE RIGOROUS APPROACH
- ◆ SHEAR WALL DESIGN SPREADSHEET

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